

subject $\xrightarrow{\text{rules}} \text{policy} \rightarrow ?$
 decision

decision sets $D_2 = \{1, 0\}$ *deny*
 \uparrow
 permit

$D_3 = \{1, 0, \perp\}$
 \uparrow
 not applicable

$D_4 = \{\phi, 0, 1, \{1, 0\}\}$

or
 $D_4 = \{P, D, NA, I\}$

$D_6 = \{P, D, NA, I, \{P\}, \{D\}, \{P, D\}\}$

\leftarrow *power set*
 $D_7 = P(D_3) \setminus \emptyset$
 $\{1\}, \{0\}, \{\perp\}, \{1, \perp\}, \{0, \perp\}, \{1, 0\}, \{1, 0, \perp\}$

weak con-/disjunction $\rightarrow \perp$ takes precedence

strong con-/disjunction $\rightarrow 0, 1$ takes precedence

D_7 : operators over D_3 extended point-wise

$$\overline{\text{op}}(X, Y) = \{\text{op}(x, y) \mid x \in X, y \in Y\}$$

	$\hat{\perp}$	1	0	\perp					
1		1	1	1					
0		1	0	\perp					
\perp		1	\perp	\perp					
	$\{1, \perp\}$	1					$\{1, \perp\}$		
	$\{0, \perp\}$	1							
	$\{1, 0\}$	1							
	$\{1, 0, \perp\}$	1						$\{1, \perp\}, \{0, \perp\}, \{1, 0, \perp\}$	

reduction of decision sets allows for re-use of operators over smaller decision sets
 as well as to enable interoperability between sets

A decision reduction maps a decision set into a smaller decision set by mapping all decisions of a set to decisions of a subset, while leaving the decisions in the subset unchanged.

A reduction is safe w.r.t. to an operator \square if and only if $p(a \square b) = p(a) \square p(b)$
 for all a and b
 in the larger decision set

a reduction is safe for a combination of operators iff it is safe for every operator individually

if two reductions are safe for an operator, their composition $p \circ p$ is also safe for that operator *note: this is a sufficient condition, but not a necessary one.*

Permit- and deny-overrides do not use a safe reduction in XACML v3.